

#### **More LMs and Naïve Bayes**

CS 780/880 Natural Language Processing Lecture 8

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#### Last lecture



Key idea: Probabilistic language modeling

#### **Concepts**

- Conditional probability
- Chain rule
- N-gram models
- Uses of language models
  - Generation
  - Evaluation
- Perplexity





**Basic idea:** model the text as the individual words occurring independently

Parametrized by corpus token frequencies

$$P(w^{(1)} \dots w^{(N)}) = \prod_{i=1}^{N} P(w^{(i)})$$

What's the problem with this?





Basic idea: model text as words being dependent on only the prior word

Parameterized by token co-occurrence frequencies

$$P(w^{(1)} \dots w^{(N)}) = \prod_{i=1}^{N} P(w^{(i)} | w^{(i-1)})$$

A bigram model is a type of **Markov Chain** 





**Enron dataset:** ~500,000 emails from Enron company, released due to scandal

My corpus: 2000 emails each sampled from the top 5 emailers

**Question:** Who sent the email "You are a huge jerk and I hate you"?



```
from nltk.util import bigrams
     # NLTK has functionality for generating all N-grams from a sequence of tokens
     list(bigrams(enron_df['tokenized'][0]))[0:10]
[('what', 'are'),
('are', 'you'),
('you', 'talking'),
('talking', 'about'),
('about', '?'),
('?', 'sandra'),
('sandra', 'dial'),
('dial', '04/24/2000'),
('04/24/2000', '03:36'),
 ('03:36', 'pm')]
```



- 1 # We'll take a look at the first email in our dataset
- 2 print(enron\_df['message\_text'][0])

What are you talking about?

```
Sandra Dial
04/24/2000 03:36 PM
To: Chris Germany/HOU/ECT@ECT
cc: Scott Hendrickson/HOU/ECT@ECT
Subject: Re: Feb 00 (RE: Voice Mail)
Scott-- Thanks.
Dude (CG),
I knew you had to be involved with this somehow.... :-)
Can you help me with this, please. Thanks. Let me know if you need more info
( I really have no more info other than this e-mail thread). Thanks man.
S
x5-7213
----- Forwarded by Sandra Dial/HOU/ECT on 04/24/2000 03:30
PM -----
Scott Hendrickson
04/24/2000 03:31 PM
To: Sandra Dial/HOU/ECT@ECT
Subject: Re: Feb 00 (RE: Voice Mail)
Well, just in that amount of time, I found out more about the deal....
I was inherited from CES. CES had originally made the sale and when we
bought their book of business, we ended up with that sale. You may want to
speak with Chris Germany about it, he was very involved with the CES
assimilation.
```

Scott



'04/24/2000']

```
# It also has functionality for adding "beginning-of-sequence" and "end-of-sequence" tokens to a
     # token sequence
    from nltk.util import pad_sequence
     list(pad_sequence(enron_df['tokenized'][0],
                       pad_left=True,
 6
                       left_pad_symbol="<s>",
                       pad_right=True,
                       right_pad_symbol="</s>",
 9
                       n=2))[0:10]
['<s>',
 'what',
 'are',
 'you',
 'talking',
 'about',
 '?',
 'sandra',
 'dial',
```



```
# Both of these utilities are packaged into a convenient pipeline
# which will take in a collection of (tokenized) texts, pad each one
# with start/end tokens, and then count all n-grams up to the number you
# give it (in our case, 2)
from nltk.lm.preprocessing import padded_everygram_pipeline

# I am training this model on just the first text
# train, vocab = padded_everygram_pipeline(2, enron_df['tokenized'][0:1])

# These things are generators, so they don't do anything until called on
print(train)
print(vocab)

* generator object padded_everygram_pipeline.<locals>.<genexpr> at 0x7cf18a443060>
```

<itertools.chain object at 0x7cf16ce91a20>



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    # give it (in our case, 2)
    # I am training this model on just the first text
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# These things are generators, so they don't do anything until called on
print(train)
# print(vocab)
```

<itertools.chain object at 0x7cf16ce91a20>



<Vocabulary with cutoff=1 unk\_label='<UNK>' and 110 items>

110

```
# Once we have training corpus and a vocabulary, we can create a MLE model to
2 # fit across it
3 from nltk.lm import MLE
   lm = MLE(2)
   #Then we fit the model
   lm.fit(train, vocab)
   print(lm.vocab)
   print(len(lm.vocab))
```

11



```
# We can look up a piece of text in the vocabulary
    lm.vocab.lookup(enron df['tokenized'][0])[0:10]
('what',
 'are',
 'you',
 'talking',
 'about',
 '?',
 'sandra',
 'dial',
 '04/24/2000',
 '03:36')
    # And any token it doesn't recognize it will replace with <UNK>
     lm.vocab.lookup(enron_df['tokenized'][1])[0:10]
('i', '<UNK>', 'we', '<UNK>', 'about', 'this', 'the', 'other', '<UNK>', '.')
```



```
# We can look up a piece of text in the vocabulary
    lm.vocab.lookup(enron df['tokenized'][0])[0:10]
('what',
 'are',
 'you',
 'talking',
 'about',
 '?',
 'sandra',
 'dial',
 '04/24/2000',
 '03:36')
    # And any token it doesn't recognize it will replace with <UNK>
     lm.vocab.lookup(enron_df['tokenized'][1])[0:10]
('i', '<UNK>', 'we', '<UNK>', 'about', 'this', 'the', 'other', '<UNK>', '.')
```



```
# We can see how many ngrams it found
    print(lm.counts)
<NgramCounter with 2 ngram orders and 443 ngrams>
    # We can count how many instances of the 'a' unigram it found
     lm.counts['the']
3
     # And how many counts of the "in that" bigram
     lm.counts[['in']]['that']
1
```



```
1  # We can look up probabilities of particular unigrams under the model!
2  lm.score('the')

0.013513513513513514

1  lm.score('a')

0.0

1  # And we can do the same for bigrams
2  lm.score('that', ['in'])

1.0
```



```
# It's often useful to report log-probabilities rather than raw probabilities
# because of underflow
| lm.logscore('the')
```

-6.209453365628949

```
# Although this can result in weird arithmatic when dealing with unknown tokens
| lm.logscore('a')
```

-inf



```
1  # Finally, we can generate new sequences according to the model
2  lm.generate(1, random_seed=3)

'00'

lm.generate(10, random_seed=7)

['</s>', '--', '--', '--', '--', '--', '--', '-', ')']
```



# Modeling our Enron data

```
from nltk.lm.preprocessing import padded_everygram_pipeline

# First I train a global model on all the emails
global_train, global_vocab = padded_everygram_pipeline(2, enron_train_df['tokenized'])

# Use a so-called "Lidstone" model to do the add-one smoothing I talked about last lecture
from nltk.lm import Lidstone
global_lm = Lidstone(order=2, gamma=1)

global_lm.fit(global_train, global_vocab)
```

```
# Here's an email generated by our global LM
display(' '.join(global_lm.generate(100, text_seed='<s>',random_seed=8)))
```

<sup>&#</sup>x27;, vladimir gorny , a consumer welfare ( hour : dicarlo , ccampbell @ ect , 2000.= if the talks between air credits will attempt to discover the escrow as of the talking to : 1.0 content-type : 7bit x-from : pverde\_5\_devers interchg\_id : can the borland database ! an gsa would remain responsible for ban kruptcy filing in abilene , john.anderson @ enron.com , '' < /o=enron/ou=na/cn=recipients/cn=pdavis1 > , sarah novosel/corp/enron @ enron.com , monika.c ausholli @ enron employees at \$ 50 books . i am on behalf of students and appointments . = and=20 electricity rates could review what .'



# Modeling our Enron data

```
# Then I try training an individual LM for each person
personal_lms = {}

from nltk.lm import Lidstone

#I use the pandas groupby function to split up the training set by name
for group_name, group_df in enron_train_df.groupby('name'):

group_train, group_vocab = padded_everygram_pipeline(2, group_df['tokenized'])
group_lm = Lidstone(order=2,gamma=12)
group_lm.fit(group_train, group_vocab) # Use the same (global) vocabulary for everyone
personal_lms[group_name] = group_lm
```

1 personal\_lms

```
{'chris': <nltk.lm.models.Lidstone at 0x7cf168b35f60>,
  'jeff': <nltk.lm.models.Lidstone at 0x7cf1683fd120>,
  'kay': <nltk.lm.models.Lidstone at 0x7cf167ba5ae0>,
  'pete': <nltk.lm.models.Lidstone at 0x7cf16722a2f0>,
  'vince': <nltk.lm.models.Lidstone at 0x7cf16729d000>}
```



# Modeling our Enron data

```
new email = "you are a huge jerk and I hate you"
     import numpy as np
     def score new email(email text:str, lm:nltk.lm.models.MLE):
       tokens = preprocess_enron(email_text) #tokenize the new email
       tokens = list(pad sequence(tokens, # add start/end tokens
                       pad_left=True,
                       left pad symbol="<s>",
 6
                       pad right=True,
                       right pad symbol="</s>",
 8
                       n=2)
       print(tokens)
10
       tokens = lm.vocab.lookup(tokens) # Look up the tokens in the vocab
11
       print(tokens)
12
       scores = []
13
       for i in range(1, len(tokens)): # Look up score of each token given previous token
14
15
         scores.append(lm.logscore(tokens[i], [tokens[i-1]]))
16
17
       return np.sum(scores), scores
```





```
for name, personal lm in personal lms.items():
      score, scores = score new email(new email, personal lm)
      print(name, np.round(score,2))
      print('\tScores',np.round(scores,2))
       print('---')
['<s>', 'you', 'are', 'a', 'huge', 'jerk', 'and', 'i', 'hate', 'you', '</s>']
('<s>', 'you', 'are', 'a', 'huge', '<UNK>', 'and', 'i', 'hate', 'you', '</s>')
chris -127.87
        Scores [-12.04 -10.31 -12.23 -13.79 -13.99 -13.99 -9.69 -13.8 -13.99 -14.01]
['<s>', 'you', 'are', 'a', 'huge', 'jerk', 'and', 'i', 'hate', 'you', '</s>']
('<s>', 'you', 'are', 'a', 'huge', 'jerk', 'and', 'i', 'hate', 'you', '</s>')
ieff -135.48
        Scores [-12.85 -11.56 -12.66 -13.88 -14.84 -14.84 -10.54 -14.74 -14.73 -14.85]
['<s>', 'you', 'are', 'a', 'huge', 'jerk', 'and', 'i', 'hate', 'you', '</s>']
('<s>', 'you', 'are', 'a', 'huge', '<UNK>', 'and', 'i', 'hate', 'you', '</s>')
kay -126.97
        Scores [-12.65 -8.78 -12.95 -13.86 -14.05 -14.05 -9.66 -13.5 -14.05 -13.41]
['<s>', 'you', 'are', 'a', 'huge', 'jerk', 'and', 'i', 'hate', 'you', '</s>']
('<s>', 'you', 'are', 'a', '<UNK>', 'And', 'i', '<UNK>', 'you', '</s>')
pete -113.7
        Scores [-11.44 -11.36 -11.36 -11.42 -11.35 -11.35 -11.36 -11.35 -11.35]
['<s>', 'you', 'are', 'a', 'huge', 'jerk', 'and', 'i', 'hate', 'you', '</s>']
('<s>', 'you', 'are', 'a', 'huge', '<UNK>', 'and', 'i', 'hate', 'you', '</s>')
vince -134.97
        Scores [-14.71 -9.92 -12.97 -14.14 -14.7 -14.7 -9.92 -14.72 -14.7 -14.5 ]
```

# Bayes Rule







When two variables may be dependent, then their joint probability is expressed as follows:

$$P(X,Y) = P(Y)P(X|Y) = P(X)P(Y|X)$$

If they happen to be independent, then P(X|Y) = P(X) and P(Y|X) = P(Y), so

$$P(X,Y) = P(Y)P(X) = P(X)P(Y)$$

# **Bayes Rule**



It follows from

that

$$P(X,Y) = P(Y)P(X|Y) = P(X)P(Y|X)$$

$$P(X|Y) = \frac{P(Y|X)P(X)}{P(Y)}$$





$$P(Lung\ cancer|Cough) = \frac{P(Cough|Lung\ cancer)P(Lung\ cancer)}{P(Cough)}$$

$$P(Conspiracy|Event) = \frac{P(Event|Conspiracy)P(Conspiracy)}{P(Event)}$$

 $P(Barista\ likes\ you|Smiles\ when\ they\ give\ you\ coffee)$   $P(Smiles\ when\ they\ give\ you\ coffee)$   $P(Smiles\ when\ they\ give\ you\ coffee)$ 

### Relative probabilities



Often we only care about the relative probability of two possible outcomes, rather than their true probability:

 $P(Lung\ cancer|Cough)\ vs.\ P(COVID|Cough)$ 

$$\frac{P(Cough|Lung\;cancer)P(Lung\;cancer)}{P(Cough)} \, \mathsf{VS.} \, \frac{P(Cough|COVID)P(COVID)}{P(Cough)}$$

Because we only care about the relative value, we can ignore the denominator

 $P(Cough|Lung\ cancer) \approx P(Cough|COVID) \approx 1.0$ 

~50 million COVID cases in 2022, ~300k new lung cancer cases in 2023

So P(COVID) = .15, and P(Lung cancer) = 0.001

So P(COVID|Cough) is **150 times** higher than  $P(Lung\ cancer|Cough)$ 

https://www.cancer.org/cancer/lung-cancer/about/key-statistics.html https://covid.cdc.gov/covid-data-tracker/#trends\_totalcases\_select\_00

### **Base rate fallacy**



A lot of fallacious thinking comes from ignoring the **base rates** P(X) and P(Y) in  $\frac{P(Y|X)P(X)}{P(Y)}$ 

$$P(Hypothesis \mid Rare\ event) = \frac{P(Rare\ event \mid Hypothesis)P(Hypothesis)}{P(Rare\ event)}$$

P(Hypothesis) is often lower than you think P(Rare event) is often higher than you think

https://en.wikipedia.org/wiki/Base\_rate\_fallacy https://en.wikipedia.org/wiki/List\_of\_cognitive\_biases

# Naïve Bayes



### **Application to text**



#### **Classification**:

 $P(Class\ 0\ |\ Words)\ vs.\ P(Class\ 1\ |\ Words)$ 

$$\frac{P(Words \mid Class \ 0)P(Class \ 0)}{P(Words)} \ \mathsf{VS.} \frac{P(Words \mid Class \ 1)P(Class \ 1)}{P(Words)}$$

We can ignore P(Words), but how do we calculate:

- $P(Words \mid Class 0)$
- P(Class 0)
- $P(Words \mid Class 1)$
- *P*(*Class* 1)

### **Application to text**



$$P(Class\ 0) = \frac{\# Class\ 0}{\# Class\ 0 + \# Class\ 1}$$

• And likewise for class 1

 $P(Words \mid Class 0)$ 

- Build an n-gram model of all texts for which class is Class 0
- Use this model to estimate  $P(Words \mid Class \ 0)$
- And likewise for Class 1

### **Naïve Bayes**



**Basic idea**: apply Bayes rule to find relative likelihoods of  $P(Class\ 0\mid Words)$  vs.  $P(Class\ 1\mid Words)$ , using **unigram model** for  $P(Words\mid Class\ C)$ 

So if we consider words =  $\{w_0, w_1, ..., wN\}$ :

$$P(Class\ 0\ |\ Words) \propto P(Class\ 0) \prod_{i=1}^{N} P(wi\ |Class\ 0)$$

$$P(Class\ 1\ |\ Words) \propto P(Class\ 1) \prod_{i=1}^{N} P(wi\ |\ Class\ 1)$$



#### **Read the SST-2 dataset**

	sentence	label
0	it 's a charming and often affecting journey .	1
1	unflinchingly bleak and desperate	0
2	allows us to hope that nolan is poised to emba	1
3	the acting , costumes , music , cinematography	1
4	it 's slow very , very slow .	0
867	has all the depth of a wading pool .	0
868	a movie with a real anarchic flair .	1
869	a subject like this should inspire reaction in	0
870	is an arthritic attempt at directing by ca	0
871	looking aristocratic, luminous yet careworn i	1



### Preprocess and vectorize the data

```
1 from nltk import PorterStemmer
1 # for this dataset, the tokenization has already been done for us
2 stemmer = PorterStemmer()
3 def preprocess(s):
4 return ' '.join([stemmer.stem(token) for token in s.strip().split(' ')])
1 train df['preprocessed'] = train df['sentence'].apply(preprocess)
2 dev df['preprocessed'] = dev df['sentence'].apply(preprocess)
1 from sklearn.feature extraction.text import CountVectorizer
1 # Why are we using a CountVectorizer here instead of TF-IDF?
3 vectorizer = CountVectorizer()
4 train X = vectorizer.fit transform(train df['preprocessed'])
5 dev X = vectorizer.transform(dev df['preprocessed'])
```



#### Build and evaluate the model

```
1 from sklearn.naive bayes import MultinomialNB
 1 # See https://scikit-learn.org/stable/modules/generated/sklearn.naive bayes.MultinomialNB.html#sklearn.naive bayes.MultinomialNB
 2 # for hyperparameter options
 4 model = MultinomialNB()
 1 model.fit(train_X, train_df['label'])
MultinomialNB()
 1 dev py = model.predict(dev X)
 1 from sklearn.metrics import accuracy score, precision score, recall score, f1 score
 1 def evaluate predictions(y, py):
     print(f'Accuracy: {accuracy score(y, py):.3f}')
     print(f'Precision: {precision_score(y, py):.3f}')
    print(f'Recall: {recall score(y, py):.3f}')
    print(f'F1: {f1_score(y, py):.3f}')
```





#### Naïve Bayes:

```
1 # Evaluating on the dev set
2 evaluate_predictions(dev_df['label'], dev_py)

Accuracy: 0.807
Precision: 0.794
Recall: 0.840
F1: 0.816

1 # Evaluating on a sample of the training set
2 train_py = model.predict(train_X[0:1000])
3 evaluate_predictions(train_df['label'].iloc[0:1000],train_py)

Accuracy: 0.891
Precision: 0.894
Recall: 0.906
F1: 0.900
```

#### K-nearest-neighbors:

```
1 evaluate_model(dev_X, dev_y, classifier)

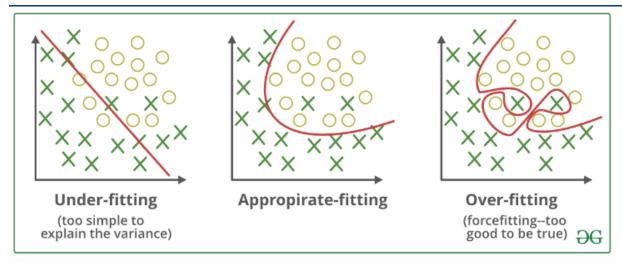
Accuracy: 0.742
Precision: 0.707
Recall: 0.842
F1: 0.769

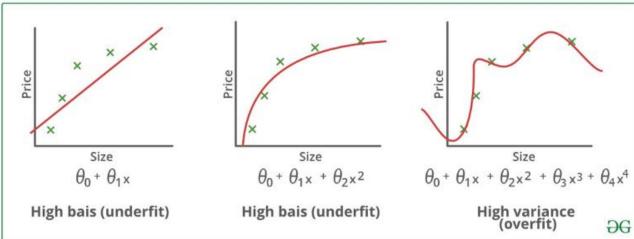
1 evaluate_model(train_X[0:1000], train_y[0:1000], classifier)

Accuracy: 0.948
Precision: 0.945
Recall: 0.959
F1: 0.952
```

# Overfitting and underfitting







**Overfitting**: model overly tuned to quirks of the training data—doesn't generalize

**Underfitted**: model not tuned enough to training data—doesn't capture data structure

Related (but not identical) to **bias- variance trade-off** 

- High bias → underfitting
- High variance → overfitting









```
1 # We can identify the words that were the biggest distinguishers by calculating
 2 # the diff between the two rows
 3 word_prob_diffs = model.feature_log_prob_[0] - model.feature_log_prob_[1]
 4 word prob diffs
array([-0.08992036, 1.41656958, -0.04909837, ..., -1.25307117,
       1.92498266, 1.04951392])
 1 # And then we can use numpy.argsort() and numpy.abs() to find the indices of the
 2 # words with the biggest diff (positive or negative)
 3 import numpy as np
 4 sorted diff indices = np.argsort(np.abs(word prob diffs))
 5 sorted diff indices
array([6103, 9942, 7833, ..., 6692, 6721, 9402])
 1 # Numpy argsort always goes in ascending order, so to get the top K indices
 2 # we have to grab the last K indices
 4 # We can use -1 as the third part of our slice, to get these back in reverse order
 5 k= 10
 6 top_k_indices = sorted_diff indices[:-k:-1]
```





```
1 # Then we can find the words and values associated with those indices
 2 vocab = vectorizer.get feature names out()
 3 top words = vocab[top k indices]
 4 top diffs = word prob diffs[top k indices]
 6 print(f'Top {k} distinguishing words in our Naive Bayes classifier')
 7 for word, diff in zip(top words, top diffs):
 8 print(f'\tWord:"{word}" - Diff: {diff:.3f}')
Top 10 distinguishing words in our Naive Bayes classifier
       Word: "unfunni" - Diff: 4.861
       Word: "poorli" - Diff: 4.698
        Word: "pointless" - Diff: 4.677
        Word: "tiresom" - Diff: 4.588
       Word: "eleg" - Diff: -4.410
        Word: "unnecessari" - Diff: 4.410
       Word: "badli" - Diff: 4.382
        Word: "embrac" - Diff: -4.355
        Word: "inept" - Diff: 4.338
```

# Interpreting log-probability differences



If:

$$\log(P(w_i|\ class\ 0)) - \log(P(w_i|\ class\ 1)) = 4.8$$

Then:

$$\frac{P(wi|class\ 0)}{P(wi|class\ 1)} = e^{4.8} = 2.718^{4.8} = 121.51$$

Meaning that w<sub>i</sub> ("unfunny" in this case) is **121.51** times more likely to occur in class 0 than in class 1



# **Explaining individual predictions**



# **Explaining individual sentences**

#### Is this overfitting?

```
1 # Then we can do the same thing as we did with the top indices above
 2 sentence words = vocab[token indices]
 3 sentence_diffs = word_prob_diffs[token_indices]
 4 print(f'Class probability differences for tokens in the sentence:')
 5 for word, diff in zip(sentence_words,sentence_diffs):
 6 print(f'\tWord:"{word}" - Diff: {diff:.3f}')
Class probability differences for tokens in the sentence:
        Word: "the" - Diff: -0.032
        Word: "movi" - Diff: 0.196
        Word: "wa" - Diff: 0.836
        Word: "pretti" - Diff: -0.643
        Word: "aw" - Diff: 1.574
        Word: "not" - Diff: 0.679
        Word: "good" - Diff: -1.021
        Word: "at" - Diff: 0.080
        Word: "all" - Diff: 0.111
```

# **Concluding thoughts**



Naïve bayes: application of Bayes Rule + unigram language modeling to classification

Huge deal in 1998

Limitations?